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The sound insulation of single leaf finite size rectangular plywood panels with orthotropic
frequency dependent bending stiffness

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ABSTRACT

Current theories for predicting the sound insulation of orthotropic materials are limited to a small range of infinite panels. This paper presents a method that allows for the prediction of the sound insulation of a finite size orthotropic panel. This method uses an equation for the forced radiation impedance of a finite size rectangular panel. This approach produces an equation which has three nested integrals. The long numerical calculation times were reduced by using approximate formulae for the azimuthally averaged forced radiation impedance. This reduced the number of nested integrals from three to two. The resulting predictions are compared to results measured using two sample sizes of four different thicknesses of plywood and one sample size of another three different thicknesses of plywood. Plywood was used for all the tests because it is somewhat orthotropic. It was found during testing that the Young's moduli of the plywood were dependent on the frequency of excitation. The influence of the frequency dependent Young's moduli was then included in the prediction method. The experimental results were also compared with a simple orthotropic prediction method.

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I. INTRODUCTION

A large number of prediction methods exist for the prediction of the sound insulation of various different partitions. A number of authors have explored the prediction of the sound transmission loss based on single leaf panels (Cremer, 1942; London, 1949; Sewell, 1970). This was also expanded to incorporate double leaf partitions (London, 1950; Sharp, 1978). A major assumption made in a number of these early models was that the panel was of infinite extent. This condition is obviously not met in any real laboratory situations.

Despite the large quantity of research that has been undertaken by a wide range of authors there are still significant gaps in the current understanding of sound insulation behaviour. Two comparative studies by Hongisto (2002; 2006) showed that the majority of the commonly used prediction methods were relatively limited in their applications and did not yield accurate results when compared to experimental results from a range of different partitions. Furthermore the evaluated models were all limited to the prediction of partitions built using isotropic materials. An equivalent study has not been performed on prediction schemes that allow for orthotropic material properties.

Several other approaches have been utilised by different authors to predict the sound insulation of single and double leaf partitions. These include finite element analysis (Trevathan, 2005; del Coz Diaz *et al.*, 2007; del Coz Diaz *et al.*, 2010), statistical energy analysis (Crocker and Price, 1969; Fahy, 1994; Steel and Craik, 1994; Craik, 1996), and transfer matrix methods (Sastry and Munjal, 1995; Lee and Xu, 2009). These methods have achieved various levels of success but were not investigated in the research presented here.

Several prediction methods presented by Hansen (1990; 1991) allow for the prediction of the sound insulation of highly orthotropic materials; corrugated sheets for example. These

materials are highly orthotropic; the stiffness in the hard direction that can be upwards of ten times the stiffness in the soft direction. This has the effect of introducing two critical frequencies that are relatively widely separated. In contrast plywood has a lower but still significant variation between the hard and soft stiffness parameters, causing the two critical frequencies to be closer together. This separation of the two critical frequencies results in two coincidence dips, with a region of reduced sound transmission loss between them.

A recent review of the vibro-acoustics of orthotropic laminates is D'Alessandro *et al.* (2013). This review references the papers of Guyader and Lesueur (1978a; 1978b; 1980) along with many other papers. Two more recent papers on the sound transmission loss of orthotropic panels are those of Woodcock and Nicolas (1995) and Kuo *et al.* (2008).

Much of the recent research on orthotropic panels has studied panels with honeycomb cores rather than the solid ply cores considered in this paper, but there are many similarities in behaviour. Orrenius *et al.* (2010) compared theoretical predictions and experimental measurements of the wave number and sound reduction index of honeycomb core panels used in aircraft fuselages and train floors. Feng and Kumar (2012) studied the fact that current theories usually predict too low a sound reduction index in the critical frequency region. Cherif and Atalla (2015) have compared theoretical predictions of a general laminate model for wave number, damping loss factor, modal density, radiation efficiency and sound reduction index with measurements often made with a number of different experimental techniques. They also derived the properties of an equivalent orthotropic panel model from the general laminate model. This equivalent orthotropic panel model was used to calculate the sound reduction index and gave better agreement with experiment for the thicker of the two honeycomb panels. The equivalent orthotropic model is used in this paper with measured properties.

The last two papers cited above each compare their theoretical predictions with two small sample size honeycomb core panels of different thickness. This paper compares its theoretical predictions with seven small sample size plywood panels of different thickness and four large sample size plywood panels of different thickness. Because plywood is not highly orthotropic, this paper also compares the experimental results with a simple isotropic model.

The prediction methods presented in this paper are built on the work undertaken by Ordubadi and Lyon (1979). The original publication by Ordubadi and Lyon presented a method for predicting the sound transmission loss of infinite orthotropic panels. In this article plywood was also utilised as a test material due to its orthotropic nature. Ordubadi and Lyon achieved reasonable agreement between the measured and predicted results, although their prediction method did not use frequency dependant material properties or the finite size of the panel. This paper uses the radiation impedance of a finite size rectangular panel and an approximation to that radiation impedance with both constant and frequency dependent Young's moduli.

II. MODEL DEVELOPMENT

The blocked incident sound pressure on the source side at the surface of the rectangle specimen mounted in an infinite rigid baffle is $2p_i$ due to the pressure doubling that occurs at the blocked surface for the plane wave sound wave with root mean square sound pressure p_i incident with an angle of incidence θ to the normal to the specimen and with an azimuthal angle ϕ to the x -axis. The transverse vibration of the specimen is accounted for by its radiation impedance $Z_w(\theta, \phi)$. The root mean square normal velocity $v(\theta, \phi)$ of the specimen is

$$v(\theta, \phi) = \frac{2p_i}{Z_p(\theta, \phi) + 2Z_w(\theta, \phi)} \quad (1)$$

where $Z_p(\theta, \phi)$ is the bending wave impedance of the plate.

The incident sound intensity $I_i(\theta, \phi)$ in the direction normal to the specimen is

$$I_i(\theta, \phi) = \frac{|p_i|^2 \cos(\theta)}{\rho_0 c} \quad (2)$$

where ρ_0 is the ambient density and c is the speed of sound of the compressible fluid on either side of the specimen. The $\cos(\theta)$ occurs because the projected area of the specimen seen from an angle of incidence of θ is proportional to $\cos(\theta)$.

The transmitted sound intensity $I_t(\theta, \phi)$ in the direction normal to the specimen is

$$I_t = \text{Re}[Z_w(\theta, \phi)] \left| \frac{2p_i}{Z_p(\theta, \phi) + 2Z_w(\theta, \phi)} \right|^2 \quad (3)$$

The sound transmission factor $\tau(\theta, \phi)$ is

$$\tau(\theta, \phi) = \frac{4\rho_0 c \text{Re}[Z_w(\theta, \phi)]}{|Z_p(\theta, \phi) + 2Z_w(\theta, \phi)|^2 \cos(\theta)} = \frac{\text{Re}\left[\frac{Z_w(\theta, \phi)}{\rho_0 c}\right]}{\left|\frac{Z_p(\theta, \phi)}{2\rho_0 c} + \frac{Z_w(\theta, \phi)}{\rho_0 c}\right|^2 \cos(\theta)} \quad (4)$$

The total incident diffuse field sound intensity I_{di} is

$$I_{di} = \int_0^{\pi/2} \int_0^{2\pi} I_i(\theta, \phi) \sin(\theta) d\phi d\theta = \frac{|p_i|^2}{\rho_0 c} \int_0^{\pi/2} \int_0^{2\pi} \cos(\theta) \sin(\theta) d\phi d\theta = \pi \frac{|p_i|^2}{\rho_0 c} \quad (5)$$

The total transmitted diffuse field sound intensity I_{dt} is

$$\begin{aligned}
 I_{dt} &= \int_0^{\pi/2} \int_0^{2\pi} \tau(\theta, \phi) I_i(\theta, \phi) \sin(\theta) d\phi d\theta \\
 &= \frac{|p_i|^2}{\rho_0 c} \int_0^{\pi/2} \int_0^{2\pi} \tau(\theta, \phi) \cos(\theta) \sin(\theta) d\phi d\theta
 \end{aligned} \tag{6}$$

The $\sin(\theta)$ term occurs in equations (5) and (6) because the amount of solid angle at an angle of θ to the normal to the specimen is proportional to $\sin(\theta)$. The diffuse field sound transmission factor τ_d is

$$\begin{aligned}
 \tau_d &= \frac{I_{dt}}{I_{di}} = \frac{1}{\pi} \int_0^{\pi/2} \int_0^{2\pi} \tau(\theta, \phi) \cos(\theta) \sin(\theta) d\phi d\theta \\
 &= \frac{1}{\pi} \int_0^{\pi/2} \int_0^{2\pi} \frac{\operatorname{Re} \left[\frac{Z_w(\theta, \phi)}{\rho_0 c} \right]}{\left| \frac{Z_p(\theta, \phi)}{2\rho_0 c} + \frac{Z_w(\theta, \phi)}{\rho_0 c} \right|^2} \sin(\theta) d\phi d\theta
 \end{aligned} \tag{7}$$

If the principal orthotropic axes and the sides of the rectangular specimen are parallel to each other and to the x and y axes, then by symmetry, the range of integration over the azimuthal angle ϕ can be reduced from the full circle to one quarter of the circle.

$$\tau_d = \frac{4}{\pi} \int_0^{\pi/2} \int_0^{\pi/2} \frac{\operatorname{Re} \left[\frac{Z_w(\theta, \phi)}{\rho_0 c} \right]}{\left| \frac{Z_p(\theta, \phi)}{2\rho_0 c} + \frac{Z_w(\theta, \phi)}{\rho_0 c} \right|^2} \sin(\theta) d\phi d\theta \tag{8}$$

The sound reduction index R is

$$R = -10 \log_{10} (\tau_d) \quad (9)$$

Thus in order to derive an expression for the transmission coefficient of a partition, expressions for both the bending wave impedance and the radiation impedance must also be derived. The bending wave impedance of an orthotropic panel can be derived from the panel's equation of motion given by Leissa (1969). This yields the following expression for the orthotropic impedance as used by Ordubadi and Lyon (1979).

$$Z_p(\theta, \phi) = \frac{k_0^4 \sin^4(\theta) B'(\phi) - \rho_s \omega^2}{i\omega} \quad (10)$$

where k_0 is the wavenumber of the incident wave, ρ_s is the surface density of the panel, ω is the angular frequency of excitation, and $B'(\phi)$ is the complex bending wave stiffness per unit width of the panel. The influence of the panel's internal damping is included in the stiffness parameter using the following equation.

$$B'(\phi) = (B_x \cos^4(\phi) + B_y \sin^4(\phi) + 2H \sin^2(\phi) \cos^2(\phi))(1 + i\eta) \quad (11)$$

where B_x and B_y are the bending wave stiffness per unit width in the orthotropic principal axes directions, H is a parameter for the orthotropic stiffness behaviour and η is the damping loss factor of the panel.

The frequency dependence of the bending stiffness properties can be incorporated by modifying equation (11). This yields the following expression

$$B'(\phi) = [B_x(f) \cos^4(\phi) + B_y(f) \sin^4(\phi) + 2H(f) \sin^2(\phi) \cos^2(\phi)][1 + i\eta] \quad (12)$$

where f is the frequency of excitation. In this paper it was assumed that the damping loss factor was independent of frequency. The value of $H(f)$ is assumed to be the geometric mean of the two orthotropic bending stiffness values, as given by

$$H(f) = \sqrt{B_x(f)B_y(f)} \quad (13)$$

The bending stiffnesses per unit width B' are derived from the Young's moduli E using the following equation.

$$B' = \frac{Eh^3}{12(1-\mu^2)} \quad (14)$$

where h is the thickness of the specimen and μ is Poisson's ratio which is assumed to be 0.3 in this paper.

The dynamic Young's moduli of the test samples were measured in the two directions parallel to the grain of the wood plies using free-free beams which were excited via force impulses. The resonant frequencies and half power bandwidths of the modes of a number of different length beams were measured. This measurement technique allowed the frequency dependence of the Young's moduli of the plywood to be measured. The frequency dependent Young's moduli were found to be approximated reasonably using a best fit exponential decay with increasing frequency. The generic expression for this model of Young's modulus is given by

$$E(f) = E_i e^{-Qf} \quad (15)$$

where $E(f)$ is the frequency dependant stiffness, E_i is the stiffness at zero frequency and Q is the rate of reduction of the stiffness parameter.

The accuracy of the model used for the frequency dependent Young's moduli has a significant impact on the predictions for the overall sound insulation. The method used to measure the dynamic Young's moduli in the research described in this paper provided relatively narrow bands of widely spaced clusters of data. The models for the frequency dependent Young's moduli were constructed from this data. This yielded models which may have had significant sources of error. This is one of the possible reasons why poor agreement may be obtained between prediction and experiment in some cases. The damping loss factor was also observed to vary with frequency, but this variation did not have a clear pattern that could be modelled effectively. Incorporating a frequency dependant damping loss factor would have a significant effect on the predicted sound insulation in and above the critical frequency region.

The finite specimen size was accounted for by using the equations for the finite panel travelling wave radiation impedance given by Davy *et al.* (2015a; 2015c). These equations involve one numerical integration and are based of the work of Rhazi and Atalla (2010). Calculating the sound reduction index, when the numerical integration is used to calculate the finite size radiation impedance, requires the numerical evaluation of three nested integrals. This means large computational times especially at higher frequencies. Thus the approximate equations of Davy *et al.* (2015a; 2015b) for the azimuthally averaged finite size radiation impedance were also used to calculate the sound reduction index. It should be noted that the use of these approximate equations means that the finite size radiation impedance is assumed to be constant as a function of azimuthal angle. The use of these approximate equations reduces the number of nested integrals that have to be numerically evaluated from three to two and

substantially speeds up the calculations. The numerical integrations were performed using Matlab's inbuilt adaptive numerical integration function, "*integral*", which uses adaptive Simpson quadrature.

Because plywood is not highly orthotropic, a simple isotropic model (Davy, 2009a) was also used to calculate the sound reduction indices. The Young's modulus used was the geometric mean of the Young's moduli in the two orthotropic principal axis directions. It was noted that the low frequency sound reduction indices calculated with the isotropic model were systematically slightly lower than those calculated using the orthotropic methods described above. Examination of the isotropic model showed it was ignoring the fluid loading on the specimen. The fluid loading on the specimen is not significant for specimens with high sound insulation, but has a significant effect for specimens with low sound insulation at low frequencies like the thinner plywood specimens studied in this paper. The fluid loading was incorporated in the isotropic model by replacing equation (42) of Davy (2009a) with equations (8) and (12) of Davy (2009b). The square root of A in equation (12) of Davy (2009b) was replaced with the length l of the side of the equivalent square given by

$$l = \frac{2l_x l_y}{l_x + l_y} \quad (16)$$

where l_x and l_y are the lengths of the sides of the rectangular specimen.

III. EXPERIMENTAL METHOD AND RESULTS

The sound insulation of a range of plywood partitions were measured for comparison with the predicted results. The partitions tested were all single leaf systems which were tested in two sizes of sound insulation facilities. The test samples were installed between a reverberation

room and a semi-anechoic room, and the intensity method was used for evaluating the sound transmission loss (ISO15186-1 (ISO, 2000)). The two sample sizes used were: 4.8×2.4 m (12 m^2) and 0.95×1.55 m (1.5 m^2), and the thicknesses measured were 7, 9, 12 and 21 mm. Plywood samples of size 0.95×1.55 m (1.5 m^2) with thicknesses of 15, 17 and 19 mm were also measured.

The small samples were clamped into a test frame using a steel box section and bolts around the perimeter. This resulted in an unsupported panel that had no studs present. The frame the sample is installed within is a heavy timber construction which is in turn bolted to a heavy concrete wall. The test aperture had a total depth of 550 mm, and the sample arrangement resulted in a source room niche depth of 350 mm.

The large samples were screwed and glued to a timber frame which was bolted into a test aperture. The edges and the joints between the panels were sealed with tape and silicone sealant. The test aperture had a total depth of 370 mm, and the sample arrangement resulted in a source room niche depth of 160 mm.

The same reverberation room was used for both sample sizes. It has a volume of 216 m^3 . Six stationary diffusing panels ensure the sound field is sufficiently diffuse. The total two-sided area of the diffusing elements is 13% of the total boundary surface area of the room. The total surface area of the reverberation room boundaries and diffusing elements is 305 m^2 . The receiving room for the small size samples was a small semi-anechoic room with a volume of 9 m^3 and a surface area of 26.4 m^2 . This room is lined with sound absorption on all the surfaces except the floor, which is covered in deep pile carpet. The semi-anechoic receiving room for the large sample sizes has a volume of 200 m^3 and a surface area of 236 m^2 . This receiving room is lined with sound absorptive materials on the walls and roof. The sound absorption in this room is

increased by the addition of numerous hanging sound absorbers resulting in a sound absorptive “tunnel”. This is projected out from the sound insulation sample to increase the absorption of the emitted sound. The floor directly in front of the sample is also treated with a large number of sound absorptive panels that are laid down to reduce unwanted reflections. The large semi-anechoic room is a rectangular parallelepiped. The reverberation room and the small semi-anechoic room would be rectangular parallelepipeds except for the fact that one of their walls is angled so that it is not parallel with its opposite wall.

The sound pressure level was measured in the reverberation source room using six Brüel and Kjær type 4189 half inch microphones. The source room was excited using a Brüel and Kjær 4269 sound source. The transmitted sound was measured on the receiving room side using a Brüel and Kjær intensity probe and Brüel and Kjær Pulse data acquisition equipment.

The intensity on the receiving room side was measured by performing two full surface scans at 150 mm from the sample surface; one horizontally and one vertically. The difference between these two scans was evaluated and the measurement was repeated if the difference was greater than one decibel in any of the one-third octave bands evaluated. The pressure-intensity index was also evaluated for each scan. If the pressure-intensity index was greater than ten decibels in any one-third octave band the scan was repeated. This procedure was repeated five times for two source locations, yielding a total of ten sound insulation measurements. These were then averaged to provide the final sound insulation.

In order to perform predictions of the sound insulation of the different thickness plywoods, their properties were required. Different estimates of these properties were made for each thickness of plywood. The Young’s moduli in both orthotropic directions and the damping loss factor were evaluated using dynamic methods. The density was measured directly. It was

found that the Young's moduli of the plywood were heavily dependent on the frequency of excitation.

The dependence of the Young's moduli on the frequency was found to be predicted with reasonable accuracy using an exponential decay. This decay curve was fitted to the frequency dependant stiffness values. An example of the curve for 12 mm plywood is shown in Figure 1. This exponential function was incorporated into the equation for the sound transmission loss as a frequency dependant parameter. However there is some scatter about the curves of best fit. This scatter is thought to be one of the reasons for the differences between the predicted and measured sound insulation.

IV. COMPARISON OF PREDICTIONS WITH EXPERIMENTAL RESULTS

The sound insulation of 7, 9, 12 and 21 mm thick plywood for the two different sample sizes and of 15, 17 and 19 mm thick plywood for the smaller sample size was predicted using four different methods described in Section II. Some of the differences between these methods are shown in Table I. The "Isotropic" method was the simple isotropic method of Davy (2009a) modified as described in Section II to include the effects of fluid loading. The "Numerical Imp." is the orthotropic method presented in Section II using numerical integration to calculate the radiation impedance. The "Approx. Imp." method is the orthotropic method presented in Section II using approximate formulae for the azimuthally averaged radiation impedance. These first three methods all use values of the Young's moduli that are constant with frequency. The "Variable E" method is the "Approx. Imp." method used with Young's moduli that vary with frequency according to best fit equations derived as described in Section II.

The comparison of these theoretical predictions with the experimental results is shown in Figure 2 to Figure 12. The four prediction methods agree well with each other for frequencies

below the critical frequency region, although the predictions of the “Isotropic model” for the large specimen size for all but the 21 mm thick plywood do appear to be slightly but systematically lower than the other predictions in this frequency range. With the exception of the large 21 mm specimen, the agreement between theory and experiment in this low frequency range is also reasonable.

The “Numerical Imp.” method and the “Approx. Imp.” method agree very well with each other across the whole of the frequency range. This is the reason why the “Approx. Imp.” method was used as the basis for the “Variable E” method. Except around the critical frequency region, the “Numerical Imp.” method and the “Approx. Imp.” method also agree well with the “Isotropic” method, except for the small systematic departure described above which occurs at low frequencies for the larger and thinner plywood specimens.

The “Variable E” method agrees better with the experimental results in the critical frequency region for the 7 and 9 mm thick plywood samples. With the exception of the large 21 mm specimen, the “Variable E” method appears to require the use of a larger damping loss factor in order to make it agree with the experimental results above the critical frequency region. Thus, again with the exception of the large 21 mm specimen, the use of Young’s moduli which do not vary with frequency gave better agreement above the critical frequency region.

All the prediction methods overestimated the depth of the critical frequency dip in the experimental data and did not always exactly predict the frequency of the minimum of the critical frequency dip, although the “Variable E” method performed better in this regard than the other three methods in the case of the 7 and 9 mm thick plywood. With the exception of the 7 mm thick plywood specimens, as expected, the “Isotropic” method predicted narrower critical frequency dips than the other orthotropic prediction methods or the experimental measurements.

With the exception of low frequency values for the large 21 mm thick specimen, all the prediction methods performed reasonably well when predicting the changes in sound insulation due to the changes in specimen area. The predicted results using the same method for the small and large specimen sizes of the same thickness converge above the critical frequency region. This trend agrees with the measured results.

All the experimental results showed ripple in the low frequency region and this was more pronounced in the case of the thicker specimens. Apart from possible experimental uncertainty, the authors are unsure why this phenomenon occurred.

In this paper, constant values of the damping loss factor as a function of frequency were used. This was also the case with the Young's moduli, except for the "Variable E" method. It appears that a more accurate determination of the variability of the Young's moduli and the damping loss factor as a function of frequency is needed in order to improve the prediction of the sound insulation of orthotropic panels like plywood.

V. SUMMARY AND CONCLUSIONS

This paper presents a method for predicting the sound insulation of finite size rectangular single leaf orthotropic panels which involves the numerical evaluation of two nested integrals. This method was used with constant Young's moduli and an exact formula for the travelling wave radiation impedance. This exact formula included one integral which need to be numerically evaluated and this led to the need to evaluate three nested integrals. The method was then used with constant Young's moduli and an approximate formula for the azimuthally averaged travelling wave radiation impedance. This reduced the number of nested integrals to two and substantially speeded up the numerical calculation. There was very little difference between the sound insulation predictions made using the exact formula and the approximate

formula. The predictions were compared with experimental sound insulation measurements on small and large specimens of four different thicknesses of plywood and on another three small specimens of other different thicknesses of plywood. Reasonable agreement was obtained except in the critical frequency region for all specimens and at low frequencies for the large specimen of the thickest plywood. A simple isotropic prediction method was also used to predict the sound insulation. This simple isotropic prediction method agreed well with the two previous predictions except in the critical frequency region where none of the three predictions agreed well with the experimental results. The simple isotropic prediction method also slightly but systematically under estimated the two previous predictions below the critical frequency region for the large specimens of the three thinnest plywood samples.

During testing of the material properties of the plywood panels, it was observed that the Young's moduli of the plywood panels were dependant on the frequency of excitation. Because of this observation, equations of best fit were derived for the Young's moduli. These equations of best fit for the Young's moduli were then used with the method presented in this paper and with the approximate formula for the azimuthally averaged travelling wave radiation impedance. The introduction of the frequency dependent Young's moduli significantly improved the predictions of sound insulation in the critical frequency region for the thinner 7 and 9 mm plywood specimens. It did not make as much difference in the critical frequency region for the other plywood specimens as had been expected. Above the critical frequency region the use of the frequency dependent Young's moduli appeared to need the use of a larger damping loss factor in order to agree with the experimental results. The one exception to this was the large 21 mm plywood specimen for which there was good agreement in this high frequency range.

It appears that a more accurate assessment of the frequency dependence of the Young's moduli and the damping loss factor may improve the prediction of the sound insulation of mildly orthotropic panels like plywood. The simple isotropic model worked better than expected except in the critical frequency region where all the prediction methods struggled, especially with the thicker plywood samples.

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TABLES

Table I. The names of the prediction methods used in this paper and the differences between them.

Prediction Method	Orthotropic	Approximate Radiation Impedance	Variable Young's Moduli
Isotropic	No	Yes	No
Numerical Imp.	Yes	No	No
Approx. Imp.	Yes	Yes	No
Variable E	Yes	Yes	Yes

FIGURE CAPTIONS

Figure 1. (Color online) Measurements of the frequency dependent Young's moduli of 12 mm plywood and the associated curves of best fit used for predicting the frequency dependent Young's moduli.

Figure 2. (Color online) Comparison of the measured and predicted sound insulation of a 7 mm thick plywood panel measuring 0.95 m wide by 1.55 m high.

Figure 3. (Color online) Comparison of the measured and predicted sound insulation of a 7 mm thick plywood panel measuring 4.8 m wide by 2.4 m high.

Figure 4. (Color online) Comparison of the measured and predicted sound insulation of a 9 mm thick plywood panel measuring 0.95 m wide by 1.55 m high.

Figure 5. (Color online) Comparison of the measured and predicted sound insulation of a 9 mm thick plywood panel measuring 4.8 m wide by 2.4 m high.

Figure 6. (Color online) Comparison of the measured and predicted sound insulation of a 12 mm thick plywood panel measuring 0.95 m wide by 1.55 m high.

Figure 7. (Color online) Comparison of the measured and predicted sound insulation of a 12 mm thick plywood panel measuring 4.8 m wide by 2.4 m high.

Figure 8. (Color online) Comparison of the measured and predicted sound insulation of a 15 mm thick plywood panel measuring 0.95 m wide by 1.55 m high.

Figure 9. (Color online) Comparison of the measured and predicted sound insulation of a 17 mm thick plywood panel measuring 0.95 m wide by 1.55 m high.

Figure 10. (Color online) Comparison of the measured and predicted sound insulation of a 19 mm thick plywood panel measuring 0.95 m wide by 1.55 m high.

Figure 11. (Color online) Comparison of the measured and predicted sound insulation of a 21 mm thick plywood panel measuring 0.95 m wide by 1.55 m high.

Figure 12. (Color online) Comparison of the measured and predicted sound insulation of a 21 mm thick plywood panel measuring 4.8 m wide by 2.4 m high.























